

- A football is kicked at 20 m/s, at an angle of 50° (above horizontal). What is the maximum range if the ball must clear a 3.0 m high bar?
- If the ball is kicked the maximum range, it will in fact impact the crossbar. What is its impact velocity?

$$v_0 = 20 \text{ m/s}$$

$$\theta = 50^\circ$$

$$v_{0x} = v_0 \cos \theta$$

$$v_{0y} = v_0 \sin \theta$$

$$a_x = 0$$

$$a_y = -9.8 \text{ m/s}^2$$

$$v_0 = 12.86 \text{ m/s}$$

$$v_0 = 15.32 \text{ m/s}$$

$$\Delta x = ?$$

$$\Delta y = 3.0 \text{ m}$$

$$t = ?$$

$$v_f^2 = v_0^2 + 2a(\Delta y)$$

$$= (15.32)^2 + 2(-9.8)(3)$$

$$v_f = \pm 13.26 \text{ m/s}$$

To find  $t$  use 2 steps  
I will show BOTH  
methods

$$v_f = v_0 + a t$$

$$-13.26 = 15.32 + (-9.8)(t)$$

$$t = 2.917 \text{ sec}$$

OR

$$\Delta y = V_0 t + \frac{1}{2} a t^2$$

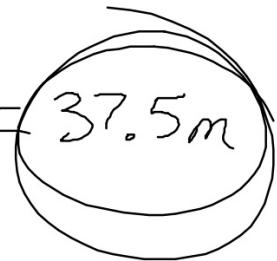
$$3 = 15.32 t - 4.9 t^2$$

then the quadratic to get  $t=2.917\text{ sec}$   
formula

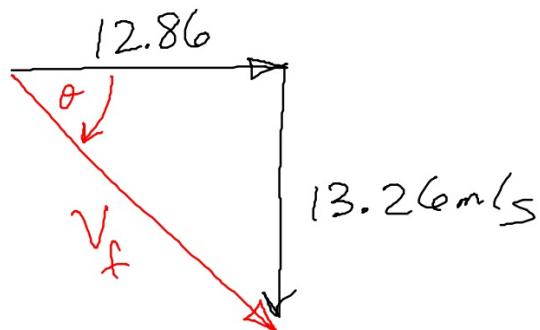
Now  $\Delta x = ?$

$$\Delta x = V_0 t + \frac{1}{2} a t^2$$

$$\Delta x = (12.86)(2.917) + 0 = 37.5\text{ m}$$



$$(\text{cont.}) \quad v_f = ? \quad v_{fx} = 12.86 \text{ m/s} \quad v_{fy} = -13.26 \text{ m/s}$$



$$\tan \theta = \frac{13.26}{12.86}$$

$$v_f^2 = 12.86^2 + 13.26^2$$

$$v_f = 18.5 \text{ m/s}, -46^\circ$$